Sirindhorn International Institute of Technology<br>Thammasat University at Rangsit<br>School of Information, Computer and Communication Technology

## ECS203: Final Examination

COURSE : ECS203 (Basic Electrical Engineering)
DATE : October 7, 2010
SEMESTER : $1 / 2010$
INSTRUCTOR: Dr. Prapun Suksompong
TIME : 9:00-12:00

| Name | ID |  |  |
| :--- | :--- | :--- | :--- |
|  | Seat |  |  |
|  |  |  |  |

## Instructions:

1. Including this cover page, there are 10 pages.
2. One A4 sheet allowed. Must be hand-written. No small pieces of paper notes glued/attached on top of it. Indicate your name and ID on the upper right corner of the sheet.
3. Read these instructions and the questions carefully.
4. Closed book. Closed notes.
5. Basic calculators are permitted, but borrowing is not allowed.
6. Allocate your time wisely. Some easy questions give many points.
7. Do not cheat. The use of communication devices including mobile phones is prohibited in the examination room.
8. Do not forget to write your first name and the last three digits of your ID on each page of your examination paper, starting from page 2 .
9. Write down all the steps that you have done to obtain your answers. You may not get any credit even when your final answer is correct without showing how you get your answer.
10. The answer(s) from earlier part(s) of a question may be useful for subsequent part(s) or question(s). You may refer to your own answer(s) from earlier part(s).
11. Units are important.
12. All phasor should be answered in polar form where the magnitude is positive and the phase is between $-180^{\circ}$ and $180^{\circ}$.
13. All sinusoid should be answered in the time-dependent cosine form where the amplitude is positive and the phase is between $-180^{\circ}$ and $180^{\circ}$.
14. Dr. Prapun will visit each exam room regularly. In general, there is no need to ask the proctor to call for Dr. Prapun.
15. Do not panic.
16. $(14 \mathrm{pt})$ Consider the circuit in Figure 1 below. Assume the switch has been at position 1 for a long time and moves to position 2 at $t=0 \mathrm{sec}$.


Figure 1
Let

$$
\mathrm{V}_{\mathrm{s} 1}=5 \mathrm{~V}, \mathrm{~V}_{\mathrm{s} 2}=0 \mathrm{~V}, \mathrm{R}_{1}=6 \Omega, \mathrm{R}_{2}=3 \Omega \text {, and } \mathrm{C}=10 \mathrm{~F} .
$$

a. (3 pt) Find $v\left(\mathbf{0}^{-}\right)$. Do not forget to justify your answer.
b. (1 pt) Find $v(0)$. Do not forget to justify your answer.
c. (4 pt) Find $v(t)$ for $t>0$.
d. (3 pt) Evaluate the amount of energy stored in the capacitor at $\mathrm{t}=15 \mathrm{sec}$.
e. (3 pt) Find $v(t)$ for $t>0$ if $\mathbf{V}_{\mathrm{s} 2}=\mathbf{1 0} \mathbf{V}$ instead of 0 V .
2. $(5 \mathrm{pt})$ Consider the circuit in Figure 2 below. Assume that the switch has been in position 1 during time $\mathrm{t}<0$. Then, during time $\mathrm{t} \geq 0$ the switch changes its position five times: at $\mathrm{t}_{1}=0, \mathrm{t}_{2}=25 \mathrm{~ms}, \mathrm{t}_{3}=50 \mathrm{~ms}, \mathrm{t}_{4}=75 \mathrm{~ms}$, and $\mathrm{t}_{5}=100 \mathrm{~ms}$.
(At time $t_{1}$, the switch changes to position 2. At time $t_{2}$, the switch changes back to position 1. At time $t_{3}$, the switch changes again to position $2 \ldots$.)


Figure 2
Let

$$
\mathrm{V}_{\mathrm{s} 1}=\mathbf{7} \mathrm{V}, \mathrm{~V}_{\mathrm{s} 2}=10 \mathrm{~V}, \mathrm{R}_{1}=6 \Omega, \mathrm{R}_{2}=3 \Omega, \text { and } \mathrm{C}=10 \mathrm{~F} .
$$

a. (3 pt) Estimate the value of $v(t)$ at time $t=\mathbf{1}$ hour.
b. (2 pt) Estimate the value of the current through the capacitor at time $t=\mathbf{1}$ hour.
3. $(10 \mathrm{pt})$ Consider the circuit in Figure 3 below. Assume the switch has been at position 1 for a long time and moves to position 2 at $\mathbf{t}=\mathbf{5} \mathbf{~ s e c}$.


Figure 3
Let

$$
\mathrm{V}_{\mathrm{s} 1}=16 \mathrm{~V}, \mathrm{~V}_{\mathrm{s} 2}=8 \mathrm{~V}, \mathrm{R}_{1}=3 \Omega, \mathrm{R}_{2}=5 \Omega \text {, and } \mathrm{C}=8 \mathrm{~F} .
$$

a. (3 pt) Find $v(0)$.
b. (2 pt) Find $v(5)$.
c. (4 pt) Find $v(t)$.
d. $(1 \mathrm{pt})$ Evaluate $v(t)$ at $\mathrm{t}=7$.
$\qquad$
4. (5 pt) Simplify $x(t)=7 \cos \left(t-777^{\circ}\right)-7 \sin \left(t-77^{\circ}\right)$. (Your answer should be a time-dependent sinusoid in standard form.)
5. ( 5 pt ) Find the sinusoid $x(t)$ which is represented by a phasor $\mathbf{X}=-7+7 j$. Assume $\omega=100 \mathrm{rad} / \mathrm{s}$. (Your answer should be a time-dependent sinusoid in standard form.)
6. (38 pt) In this question, you must use the specified techniques to solve the problem. There will be no credit given if you do not follow the instructions. As always, your score depends strongly on your explanation of your answer. If the explanation is incomplete, zero score may be given even when the final answer is correct.

Consider the circuit below.


Figure 4
Suppose

$$
\begin{gathered}
v_{s}(t)=7 \cos \left(200 t+30^{\circ}\right) \mathrm{V}, \\
\mathrm{R}_{1}=6 \Omega, \mathrm{R}_{2}=4 \Omega, \text { and } L=5 \mathrm{mH} .
\end{gathered}
$$

a. (1 pt) Find $\mathbf{V}_{\mathbf{s}}$ (which is the phasor representation of $\mathrm{v}_{\mathrm{s}}(\mathrm{t})$ ).
b. (2 pt) Find the impedance of the inductor.
c. (8 pt) Use mesh analysis to find all mesh currents (in the clockwise direction) in phasor form.
d. $(2 \mathrm{pt})$ Use the mesh current(s) to find the current $i_{L}(t)$ through the inductor.
e. (6 pt) Use nodal analysis to find the voltage $v_{2}(t)$ across the resistor $\mathrm{R}_{2}$.
f. $(4 \mathrm{pt})$ Find the voltage $v_{1}(t)$ across the resistor $\mathrm{R}_{1}$.
g. (5 pt) Use source transformation(s) and/or impedance combination(s) to transform the part of the circuit to the left of the inductor into a phasor voltage source $\mathbf{V}_{\mathbf{A}}$ in series with an impedance $\mathbf{Z}_{\mathbf{A}}$.
h. (3 pt) Use $\mathbf{V}_{\mathbf{A}}, \mathbf{Z}_{\mathbf{A}}$, and the impedance of the inductor to find $i_{L}(t)$.
i. (1 pt) Find the instantaneous power absorbed by $\mathrm{R}_{1}$
j. (1 pt) Find the average power absorbed by $\mathrm{R}_{1}$
k. (2 pt) Find the average power absorbed by L

1. (3 pt) Find the average power absorbed by the voltage source.
2. $(9 \mathrm{pt})$ Consider the circuit in Figure 5 below.


Figure 5
Suppose

$$
v_{s}(t)=7 \cos \left(200 t+30^{\circ}\right) \mathrm{V},
$$

a. (4 pt) Determine the load impedance $\mathrm{Z}_{\mathrm{L}}$ for maximum power transfer (to $\left.Z_{L}\right)$.
b. (3 pt) In the lab, how can you build the optimal $\mathrm{Z}_{\mathrm{L}}$ which you got in part (a) from a combination of resistor/inductor/capacitor? Draw and explain your answer. Indicate the values of each component (in $\Omega / H / F$ ).
c. $(2 \mathrm{pt})$ Calculate the maximum power absorbed by the load $\mathrm{Z}_{\mathrm{L}}$.
8. ( 3 pt ) What is seriously wrong with Figure 6 below. Justify your answer.


Figure 6
9. $(4 \mathrm{pt})$ Consider the circuit in Figure 7.


Figure 7


Figure 8

Assume that the switch has been in position 1 during time $t<0$. Then, during time $t \geq 0$ the switch changes its position three times: at $t_{1}, t_{2}, t_{3}$.
(At time $t_{1}$, the switch changes to position 2. At time $t_{2}$, the switch changes back to position 1. At time $t_{3}$, the switch changes again to position 2.)

Figure 8 shows the voltage $v(t)$ for time $t>0$.
$\qquad$

If the capacitance value $C$ is decreased by $10 \%$, how would the plot in Figure 8 change? Provide some explanation and sketch the plot of the new $v(t)$ directly in Figure 8. Assume the same initial voltage at time $t_{1}$.
10. (6 pt) Consider the op-amp circuit in Figure 9 below. All voltages are represented by their phasors.


Figure 9
a. (5 pt) Find the gain $\left|\frac{\mathbf{V}_{\text {out }}}{\mathbf{V}_{\text {in }}}\right|$ in terms of $\omega, \mathrm{R}, \mathrm{C}, \mathrm{R}_{\mathrm{p}}$.
b. (1 pt) Find the gain $\left|\frac{\mathbf{V}_{\text {out }}}{\mathbf{V}_{\text {in }}}\right|$ when $\omega=0 \mathrm{rad} / \mathrm{s}$.

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[^0]:    11. (1 pt) Do not forget to submit your formula sheet with your final exam.
